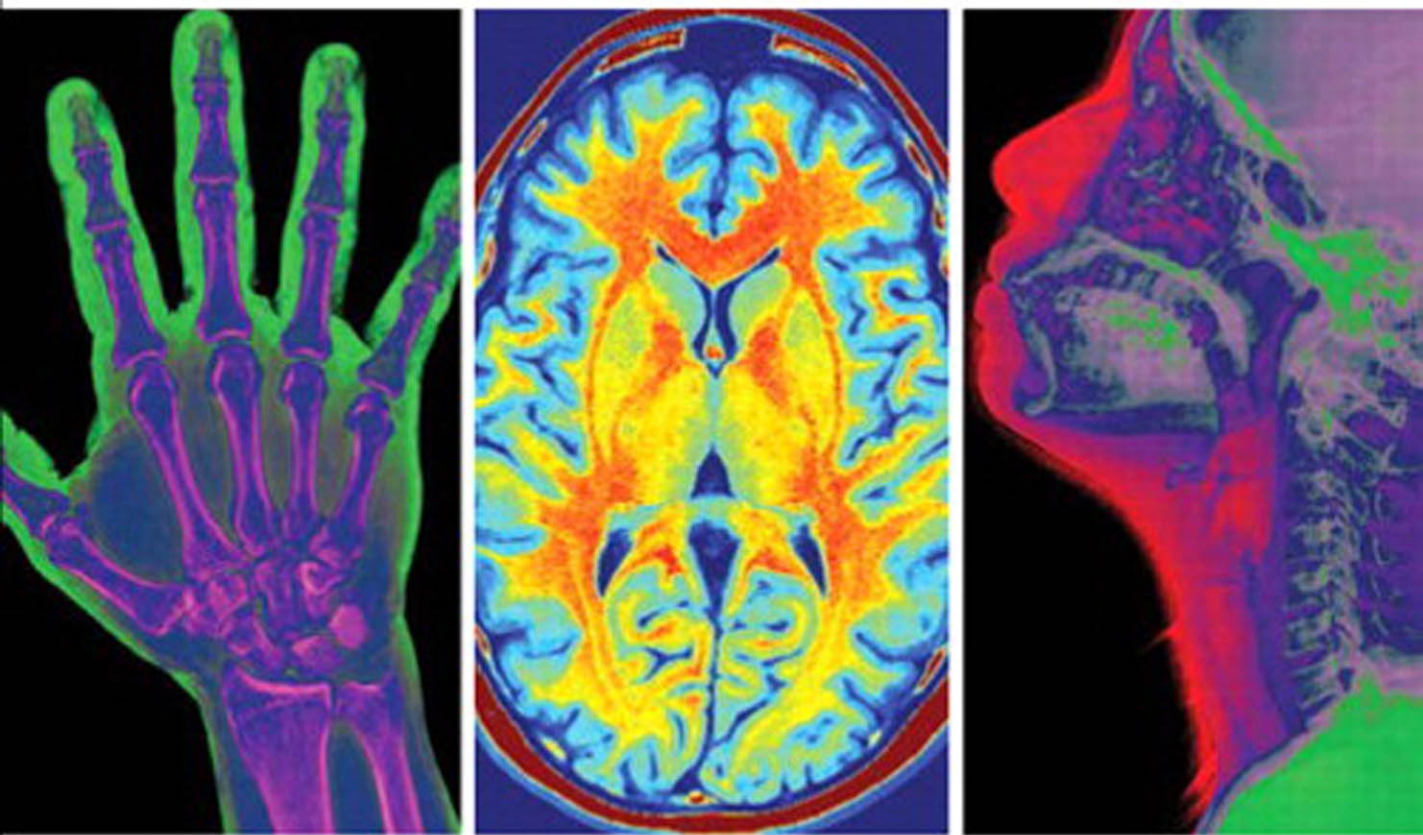


MEDICAL IMAGING

SIGNALS AND SYSTEMS

SECOND EDITION



JERRY L. PRINCE
JONATHAN M. LINKS

Medical Imaging Signals and Systems

This page intentionally left blank

Medical Imaging Signals and Systems

Jerry L. Prince

*Electrical and Computer Engineering
Whiting School of Engineering
Johns Hopkins University*

Jonathan M. Links

*Environmental Health Sciences
Bloomberg School of Public Health
Johns Hopkins University*

PEARSON

Boston Columbus Indianapolis New York San Francisco Upper Saddle River
Amsterdam Cape Town Dubai London Madrid Milan Munich Paris Montréal Toronto
Delhi Mexico City São Paulo Sydney Hong Kong Seoul Singapore Taipei Tokyo

Vice President and Editorial
Director, ECS: *Marcia J. Horton*
Executive Editor: *Holly Stark*
Marketing Manager: *Tim Galligan*
Marketing Assistant: *Jon Bryant*
Senior Managing Editor: *Scott Disanno*
Project Manager: *Irwin Zucker*
Art Director: *Jayne Conte*
Cover Designer: *Bruce Kenselaar*

Cover Image: From left to right: X-ray image
of the hand, MRI cross section of the brain,
X-ray image of the head and neck.
Photos Courtesy of GE Healthcare.
Full-Service Project Management/
Composition: *SPI Global*
Printer/Binder: *Courier Kendallville*
Cover Printer: *Courier Kendallville*

Credits and acknowledgments borrowed from other sources and reproduced, with permission, in this textbook appear on appropriate page within text.

Copyright © 2015, 2006 by Pearson Education, Inc., publishing as Prentice Hall, 1 Lake Street, Upper Saddle River, NJ 07458.

All rights reserved. Manufactured in the United States of America. This publication is protected by Copyright, and permission should be obtained from the publisher prior to any prohibited reproduction, storage in a retrieval system, or transmission in any form or by any means, electronic, mechanical, photocopying, recording, or likewise. To obtain permission(s) to use material from this work, please submit a written request to Pearson Education, Inc., Permissions Department, imprint permissions address.

Many of the designations by manufacturers and seller to distinguish their products are claimed as trademarks. Where those designations appear in this book, and the publisher was aware of a trademark claim, the designations have been printed in initial caps or all caps.

The author and publisher of this book have used their best efforts in preparing this book. These efforts include the development, research, and testing of the theories and programs to determine their effectiveness. The author and publisher make no warranty of any kind, expressed or implied, with regard to these programs or the documentation contained in this book. The author and publisher shall not be liable in any event for incidental or consequential damages in connection with, or arising out of, the furnishing, performance, or use of these programs.

Library of Congress Cataloging-in-Publication Data

Prince, Jerry L., author.
Medical imaging signals and systems / Jerry L. Prince, Jonathan M. Links. –2.
p. ; cm.
Includes bibliographical references and index.
ISBN 978-0-13-214518-3 (alk. paper)
I. Links, Jonathan M., author. II. Title.
[DNLM: 1. Diagnostic Imaging. 2. Signal Processing, Computer-Assisted. WN 180]
RC78.7.D53
616.07'54–dc23

2014000639

10 9 8 7 6 5 4 3 2 1

PEARSON

ISBN 10: 0-13-214518-9
ISBN 13: 978-0-13-214518-3

*To our families
Carol, Emily, Ben, Mark, and David
Laura, Annie, and Beth
who help us see what's important and what's not.*

This page intentionally left blank

Contents

Preface xv

Part I Basic Imaging Principles 1

1

Introduction 5

- 1.1 History of Medical Imaging 5
- 1.2 Physical Signals 6
- 1.3 Imaging Modalities 7
- 1.4 Projection Radiography 7
- 1.5 Computed Tomography 9
- 1.6 Nuclear Medicine 10
- 1.7 Ultrasound Imaging 11
- 1.8 Magnetic Resonance Imaging 12
- 1.9 Multimodality Imaging 13
- 1.10 Summary and Key Concepts 13

2

Signals and Systems 15

- 2.1 Introduction 15
- 2.2 Signals 16
 - 2.2.1 Point Impulse 16
 - 2.2.2 Line Impulse 19
 - 2.2.3 Comb and Sampling Functions 19
 - 2.2.4 Rect and Sinc Functions 20
 - 2.2.5 Exponential and Sinusoidal Signals 22
 - 2.2.6 Separable Signals 23
 - 2.2.7 Periodic Signals 23
- 2.3 Systems 24
 - 2.3.1 Linear Systems 24
 - 2.3.2 Impulse Response 25
 - 2.3.3 Shift Invariance 25
 - 2.3.4 Connections of LSI Systems 28

2.3.5	Separable Systems	30
2.3.6	Stable Systems	31
2.4	The Fourier Transform	31
2.5	Properties of the Fourier Transform	36
2.5.1	Linearity	36
2.5.2	Translation	37
2.5.3	Conjugation and Conjugate Symmetry	37
2.5.4	Scaling	37
2.5.5	Rotation	38
2.5.6	Convolution	38
2.5.7	Product	39
2.5.8	Separable Product	40
2.5.9	Parseval's Theorem	40
2.5.10	Separability	40
2.6	Transfer Function	41
2.7	Circular Symmetry and the Hankel Transform	43
2.8	Summary and Key Concepts	47

3

Image Quality 54

3.1	Introduction	54
3.2	Contrast	55
3.2.1	Modulation	56
3.2.2	Modulation Transfer Function	56
3.2.3	Local Contrast	60
3.3	Resolution	61
3.3.1	Line Spread Function	61
3.3.2	Full Width at Half Maximum	62
3.3.3	Resolution and Modulation Transfer Function	63
3.3.4	Subsystem Cascade	65
3.3.5	Resolution Tool	68
3.3.6	Temporal and Spectral Resolution	68
3.4	Noise	69
3.4.1	Random Variables	70
3.4.2	Continuous Random Variables	70
3.4.3	Discrete Random Variables	72
3.4.4	Independent Random Variables	75
3.5	Signal-to-Noise Ratio	76
3.5.1	Amplitude SNR	77
3.5.2	Power SNR	77
3.5.3	Differential SNR	79
3.5.4	Decibels	80
3.6	Sampling	80
3.6.1	Signal Model for Sampling	81
3.6.2	Nyquist Sampling Theorem	83
3.6.3	Anti-Aliasing Filters	85

- 3.7 Other Effects 86
 - 3.7.1 Artifacts 86
 - 3.7.2 Distortion 88
- 3.8 Accuracy 88
 - 3.8.1 Quantitative Accuracy 89
 - 3.8.2 Diagnostic Accuracy 89
- 3.9 Summary and Key Concepts 92

Part II Radiographic Imaging 101

4

Physics of Radiography 106

- 4.1 Introduction 106
- 4.2 Ionization 107
 - 4.2.1 Atomic Structure 107
 - 4.2.2 Electron Binding Energy 109
 - 4.2.3 Ionization and Excitation 109
- 4.3 Forms of Ionizing Radiation 110
 - 4.3.1 Particulate Radiation 110
 - 4.3.2 Electromagnetic Radiation 112
- 4.4 Nature and Properties of Ionizing Radiation 113
 - 4.4.1 Primary Energetic Electron Interactions 114
 - 4.4.2 Primary Electromagnetic Radiation Interactions 116
- 4.5 Attenuation of Electromagnetic Radiation 120
 - 4.5.1 Measures of X-Ray Beam Strength 121
 - 4.5.2 Narrow Beam, Monoenergetic Photons 123
 - 4.5.3 Narrow Beam, Polyenergetic Photons 125
 - 4.5.4 Broad Beam Case 127
- 4.6 Radiation Dosimetry 127
 - 4.6.1 Exposure 127
 - 4.6.2 Dose and Kerma 128
 - 4.6.3 Linear Energy Transfer (LET) 128
 - 4.6.4 The *f*-Factor 128
 - 4.6.5 Dose Equivalent 129
 - 4.6.6 Effective Dose 130
- 4.7 Summary and Key Concepts 131

5

Projection Radiography 135

- 5.1 Introduction 135
- 5.2 Instrumentation 136
 - 5.2.1 X-Ray Tubes 136
 - 5.2.2 Filtration and Restriction 139

- 5.2.3 Compensation Filters and Contrast Agents 141
- 5.2.4 Grids, Airgaps, and Scanning Slits 143
- 5.2.5 Film-Screen Detectors 146
- 5.2.6 X-Ray Image Intensifiers 148
- 5.2.7 Digital Radiography 149
- 5.2.8 Mammography 154
- 5.3 Image Formation 154
 - 5.3.1 Basic Imaging Equation 154
 - 5.3.2 Geometric Effects 155
 - 5.3.3 Blurring Effects 162
 - 5.3.4 Film Characteristics 166
- 5.4 Noise and Scattering 169
 - 5.4.1 Signal-to-Noise Ratio 169
 - 5.4.2 Quantum Efficiency and Detective Quantum Efficiency 171
 - 5.4.3 Compton Scattering 173
- 5.5 Summary and Key Concepts 175

6

Computed Tomography 186

- 6.1 Introduction 186
- 6.2 CT Instrumentation 188
 - 6.2.1 CT Generations 188
 - 6.2.2 X-Ray Source and Collimation 194
 - 6.2.3 Dual-Energy CT 194
 - 6.2.4 CT Detectors 195
 - 6.2.5 Gantry, Slip Ring, and Patient Table 196
- 6.3 Image Formation 197
 - 6.3.1 Line Integrals 197
 - 6.3.2 CT Numbers 198
 - 6.3.3 Parallel-Ray Reconstruction 198
 - 6.3.4 Fan-Beam Reconstruction 208
 - 6.3.5 Helical CT Reconstruction 212
 - 6.3.6 Cone Beam CT 213
 - 6.3.7 Iterative Reconstruction 213
- 6.4 Image Quality in CT 213
 - 6.4.1 Resolution 214
 - 6.4.2 Noise 216
 - 6.4.3 Artifacts 221
- 6.5 Summary and Key Points 223

Part III Nuclear Medicine Imaging 235

7

The Physics of Nuclear Medicine 239

- 7.1 Introduction 239
- 7.2 Nomenclature 240
- 7.3 Radioactive Decay 240
 - 7.3.1 Mass Defect and Binding Energy 240
 - 7.3.2 Line of Stability 242
 - 7.3.3 Radioactivity 243
 - 7.3.4 Radioactive Decay Law 243
- 7.4 Modes of Decay 245
 - 7.4.1 Positron Decay and Electron Capture 245
 - 7.4.2 Isomeric Transition 246
- 7.5 Statistics of Decay 247
- 7.6 Radiotracers 249
- 7.7 Summary and Key Concepts 251

8

Planar Scintigraphy 255

- 8.1 Introduction 255
- 8.2 Instrumentation 255
 - 8.2.1 Collimators 256
 - 8.2.2 Scintillation Crystal 258
 - 8.2.3 Photomultiplier Tubes 258
 - 8.2.4 Positioning Logic 260
 - 8.2.5 Pulse Height Analyzer 260
 - 8.2.6 Gating Circuit 262
 - 8.2.7 Image Capture 263
 - 8.2.8 Solid State and Other New Cameras 264
- 8.3 Image Formation 264
 - 8.3.1 Event Position Estimation 264
 - 8.3.2 Acquisition Modes 266
 - 8.3.3 Anger Camera Imaging Equation 269
- 8.4 Image Quality 272
 - 8.4.1 Resolution 273
 - 8.4.2 Sensitivity 276
 - 8.4.3 Uniformity 278
 - 8.4.4 Energy Resolution 279

- 8.4.5 Noise 280
- 8.4.6 Factors Affecting Count Rate 281
- 8.5 Summary and Key Concepts 282

9

Emission Computed Tomography 293

- 9.1 Instrumentation 294
 - 9.1.1 SPECT Instrumentation 294
 - 9.1.2 PET Instrumentation 298
- 9.2 Image Formation 304
 - 9.2.1 SPECT Image Formation 304
 - 9.2.2 PET Image Formation 309
 - 9.2.3 Iterative Reconstruction 313
- 9.3 Image Quality in SPECT and PET 317
 - 9.3.1 Spatial Resolution 318
 - 9.3.2 Attenuation and Scatter 319
 - 9.3.3 Random Coincidences 320
 - 9.3.4 Contrast 320
 - 9.3.5 Noise and Signal-to-Noise Ratio 321
- 9.4 Summary and Key Concepts 321

Part IV Ultrasound Imaging 331

10

The Physics of Ultrasound 335

- 10.1 Introduction 335
- 10.2 The Wave Equation 336
 - 10.2.1 Three-Dimensional Acoustic Waves 336
 - 10.2.2 Plane Waves 338
 - 10.2.3 Spherical Waves 340
- 10.3 Wave Propagation 341
 - 10.3.1 Acoustic Energy and Intensity 341
 - 10.3.2 Reflection and Refraction at Plane Interfaces 342
 - 10.3.3 Transmission and Reflection Coefficients at Plane Interfaces 343
 - 10.3.4 Attenuation 344
 - 10.3.5 Scattering 347
 - 10.3.6 Nonlinear Wave Propagation 347
- 10.4 Doppler Effect 349

- 10.5 Beam Pattern Formation and Focusing 353
 - 10.5.1 Simple Field Pattern Model 354
 - 10.5.2 Diffraction Formulation 355
 - 10.5.3 Focusing 361
- 10.6 Summary and Key Concepts 362

11

Ultrasound Imaging Systems 367

- 11.1 Introduction 367
- 11.2 Instrumentation 367
 - 11.2.1 Ultrasound Transducer 367
 - 11.2.2 Ultrasound Probes 372
- 11.3 Pulse-Echo Imaging 374
 - 11.3.1 The Pulse-Echo Equation 374
- 11.4 Transducer Motion 377
- 11.5 Ultrasound Imaging Modes 380
 - 11.5.1 A-Mode Scan 380
 - 11.5.2 M-Mode Scan 381
 - 11.5.3 B-Mode Scan 381
- 11.6 Steering and Focusing 386
 - 11.6.1 Transmit Steering and Focusing 386
 - 11.6.2 Beamforming and Dynamic Focusing 388
- 11.7 Three-Dimensional Ultrasound Imaging 391
- 11.8 Image Quality 392
 - 11.8.1 Resolution 392
 - 11.8.2 Noise and Speckle 395
- 11.9 Summary and Key Concepts 396

Part V Magnetic Resonance Imaging 407

12

Physics of Magnetic Resonance 410

- 12.1 Introduction 410
- 12.2 Microscopic Magnetization 410
- 12.3 Macroscopic Magnetization 412
- 12.4 Precession and Larmor Frequency 414
- 12.5 Transverse and Longitudinal Magnetization 416
 - 12.5.1 NMR Signals 417
 - 12.5.2 Rotating Frame 419

- 12.6 RF Excitation 419
- 12.7 Relaxation 422
- 12.8 The Bloch Equations 425
- 12.9 Spin Echoes 426
- 12.10 Basic Contrast Mechanisms 429
- 12.11 Summary and Key Concepts 433

13

Magnetic Resonance Imaging 439

- 13.1 Instrumentation 439
 - 13.1.1 System Components 439
 - 13.1.2 Magnet 441
 - 13.1.3 Gradient Coils 442
 - 13.1.4 Radio Frequency Coils 445
 - 13.1.5 Scanning Console and Computer 446
- 13.2 MRI Data Acquisition 447
 - 13.2.1 Encoding Spatial Position 447
 - 13.2.2 Slice Selection 449
 - 13.2.3 Frequency Encoding 455
 - 13.2.4 Polar Scanning 460
 - 13.2.5 Gradient Echoes 461
 - 13.2.6 Phase Encoding 462
 - 13.2.7 Spin Echoes 465
 - 13.2.8 Pulse Repetition Interval 467
 - 13.2.9 Realistic Pulse Sequences 467
- 13.3 Image Reconstruction 469
 - 13.3.1 Rectilinear Data 470
 - 13.3.2 Polar Data 471
 - 13.3.3 Imaging Equations 472
- 13.4 Image Quality 475
 - 13.4.1 Sampling 475
 - 13.4.2 Resolution 477
 - 13.4.3 Noise 479
 - 13.4.4 Signal-to-Noise Ratio 481
 - 13.4.5 Artifacts 482
- 13.5 Advanced Contrast Mechanisms 483
- 13.6 Summary and Key Concepts 487

Index 497

Preface

Although the underlying principles of medical imaging have not changed in the nine years since the first edition of this book was published, the instrumentation and practices have continued to evolve and improve. This second edition maintains the *signals and systems* focus of the first edition, with up-to-date descriptions of instrumentation. We still cover the most important *imaging modalities* in radiology: projection radiography, x-ray computed tomography, nuclear medicine scintigraphy and emission tomography, ultrasound imaging, and magnetic resonance imaging. But we now provide additional material on digital radiography, multi-row detector CT systems, 3D ultrasound, both functional and diffusion-weighted magnetic resonance imaging, and much more. As before, we expect the reader to be familiar with signals and systems, which are usually covered in the sophomore year of most engineering curricula, and with elementary probability. Freshman courses in physics, chemistry, and calculus are also assumed.

As with the first edition, the book is organized into parts emphasizing key overall conceptual divisions. Part I introduces basic imaging principles, including an introduction to medical imaging systems in Chapter 1, a review of signal processing (with emphasis on two-dimensional signals) in Chapter 2, and a discussion of image quality in Chapter 3. Our presentation of the theory of medical imaging systems is strongly based on continuous signals; however, a development of discrete signals is included to permit discussions on sampling and implementation. Issues of image quality, including resolution, noise, contrast, geometric distortion, and artifacts are described in a general context here, and are revisited within each modality in subsequent chapters.

Part II describes key modalities in radiographic imaging. It begins in Chapter 4 with a brief presentation of the physics of radiography, including the generation and detection of ionizing radiation and its effect on the human body. Chapter 5 describes projection radiography systems, including chest x-ray, fluoroscopy, and mammography systems. As in all subsequent chapters, coverage focuses on signals, including only enough physics and biology to motivate the modality and provide a model for the analysis. Chapter 5 also presents the mathematics of *projection imaging*, a very fundamental idea in medical imaging. Chapter 6 covers x-ray computed tomography, expanding on the instrumentation and mathematics of projection imaging and introducing the concept of image reconstruction in medical imaging. Computed tomography produces true *tomograms* (images of cross sections of the body) rather than projections of the body.

Part III presents the physics and modalities of nuclear medicine imaging. Chapter 7 describes the physics of nuclear medicine, focusing primarily on the concept of radioactivity. The major modalities in nuclear medicine imaging are described in Chapter 8, which covers planar scintigraphy, and Chapter 9, which covers emission computed tomography.

Part IV covers ultrasound imaging. It begins in Chapter 10 with a brief presentation of the physics of sound, and continues in Chapter 11 with the various imaging modes offered within this rich modality. Part V covers magnetic resonance imaging. Chapter 12 presents the physics of nuclear magnetic resonance, and Chapter 13 continues with a presentation of various magnetic resonance imaging techniques.

We have used the first edition of this book for a one-semester upper-level/graduate course on medical imaging systems. In order to cover the material in one semester, we routinely skip some material in the book, and we move at a very brisk pace. Although it was very tempting to add more depth in modern instrumentation, reconstruction methods, and diagnostic uses of medical imaging, we feel that this breadth of material could not be covered in one semester with sufficient depth, and would be inconsistent with our primary goal of providing a unified view of medical imaging from a signals and systems point of view. On the other hand, we feel that this book could be used as the basis for a two-semester course, perhaps by covering Parts I–III in the first semester and Parts IV–V in the second semester. A two-semester approach would allow instructors to use supplementary materials for additional depth in the physics and instrumentation of medical imaging, or to present current research topics.

Medical imaging is very visual—just ask any radiologist. Although the formalism of signals and systems is mathematical, we understand the advantages offered through visualization. Therefore, the book contains many images and diagrams. Some are strictly pedagogical, offered in conjunction with the exposition or an example problem. Others are motivational, revealing interesting features for discussion or study. Special emphasis is made to provide biologically relevant examples, so that the important context of medical imaging can be appreciated by students. Many images have been added or replaced in this edition, in order to provide better coverage of current use and to provide reference images to help explain features and qualities of the various modalities.

New to This Edition

The second edition of this book arose primarily from the need to provide updates to the technology and methods in medical imaging systems, which have undergone substantial development since the first edition. At the same time, we were able to incorporate changes to the organization of the book and to improve certain aspects of pedagogy. Instructors and students alike now have more modern material from the core medical imaging modalities while still maintaining the signal processing perspective in a unified treatment of medical imaging signal and systems.

The most significant changes to this new edition include:

- Completely rewritten overview sections including many new images to better motivate and explain the core modalities that use x-rays, radioactivity, ultrasound, and nuclear magnetic resonance.
- New sections on digital radiography systems and mammography in projection radiography.
- A new section on multi-row detectors in computed tomography.

- A new section on iterative reconstruction in emission tomography in nuclear medicine.
- New sections on nonlinear wave propagation and harmonic imaging in ultrasound imaging.
- New development and presentation of imaging equations in planar scintigraphy, single photon emission computed tomography, and positron emission tomography.
- New sections on three-dimensional imaging, noise, and speckle in ultrasound imaging.
- New sections on susceptibility weighted imaging, functional magnetic resonance imaging, and diffusion magnetic resonance imaging in magnetic resonance imaging.
- Reorganization of the chapters on signals and systems and image quality to encourage a better pedagogical flow.
- Many new problems, added primarily to the chapters having relatively fewer problems in the first edition. There are a total of 261 problems in this second edition.

Acknowledgments

Many students, friends, colleagues, and teaching assistants contributed to this book through discussions and critiques. We wish to thank Elliot R. McVeigh and John I. Goutsias, who co-taught our course at Johns Hopkins University during the early years and helped draft the first edition of the book. We are grateful to Drs. Avneesh Chhabra, Harvey Ziessman, Peter Calabresi, and David Yousem for providing several clinical images (and their descriptions) and to Vince Blasko and Beatrice Mudge for providing several images depicting artifacts that can arise in clinical imaging. Xiao Han, Xiaodong Tao, Li Pan, Vijay Parthasarathy, Tara Johnson, Minnan Xu, Abd El-Monem El-Sharkawy, Kahaled Abd-Elmoniem, Lotta Ellingsen, Jing Wan, Snehashis Roy, Harsh Agarwal, Issel Lim, Xian Fan, Nan Li, Sahar Soleimanifard, Nathanel Kuo, Jeffrey Pompe, Min Chen, Chuyang Ye, and Zhen Yang contributed problems and solutions, Dhruv Lamba helped find new images, and Aaron Carass fixed many LaTeX problems. We are grateful for the images provided to us by GE Healthcare, Philips Healthcare, and Osirix. We thank J. Webster Stayman for reviewing the digital radiography section. We would also like to thank six anonymous reviewers who provided comments on their experiences with the first edition, which provided a basis for many of the changes we have made to this edition, and five anonymous reviewers who reviewed a draft of this edition, which helped us to better balance material in several sections. Finally, we would like to thank Dr. William R. Brody, who inspired the creation of the course out of which this book emerged.

JERRY L. PRINCE
JONATHAN M. LINKS

This page intentionally left blank

Basic Imaging Principles

P A R T



Overview

What does the human body look like *on the inside*? The smart answer: It depends on how you look at it. The most direct way to look inside the human body is to cut it open, for example, through surgery. A refinement of this procedure might be to use an endoscope, essentially a light tube that is “threaded” through the body, which conveys an image to a display device. Both methods offer direct optical viewing, but also involve cutting the body, putting something in it, or both. These are *invasive techniques*, which cause (potential) damage or trauma to the body.

The beauty of medical imaging is that we can see inside the human body in ways that are less invasive than surgery or endoscopy. In some cases—for example, magnetic resonance imaging (MRI) and ultrasound imaging—the methods are completely *noninvasive* and risk-free so far as we know. In other cases—for example, projection radiography, x-ray computed tomography (CT), and nuclear medicine—there is some risk associated with the radiation exposure, even though these methods are considered noninvasive as well.

Fundamentally, these medical imaging techniques mean that we do not need to cut the body or put a physical device into it in order to “see inside.” Of perhaps even greater importance, these techniques allow us to see things that are not visible to the naked eye in the first place. For example, functional magnetic resonance imaging (fMRI) allows us to obtain images of organ perfusion or blood flow, and positron emission tomography (PET) allows us to obtain images of metabolism or receptor binding. In other words, the various imaging techniques allow us to see inside the body in different ways—the “signal” is different in each case and can reveal information which the other methods cannot. Each of these different methods is a different *imaging modality*, and the “signals” that arise are intrinsically different. This hearkens back to the opening question: What does the human body look like on the inside? The answer: It depends on the measured signal of interest.

In this book, we use a *signals and systems* approach to explain and analyze the most common imaging methods in radiology today. We want to answer the question: What do the images look like and why? We will discover that medical imaging physics allows us to image certain parameters of the body's tissues, such as reflectivity in ultrasound imaging, linear attenuation coefficient in computed tomography, and hydrogen proton density in magnetic resonance imaging. These physical parameters, which one can think of as "signals" within the body, represent the input signal into an imaging system. In medical imaging, the "object" or "signal" arising from the patient depends on the physical processes governing a given imaging modality. Thus, a given patient represents an ensemble of different objects or signals. In considering a given medical image, it is thus important to start with the physics that underlie the creation of signals from the patient for that modality. Accordingly, each part of this book is organized such that the first chapter describes the relevant physics, and subsequent chapters describe those modalities based on the specific physical processes of that part.

The first output of any medical imaging system is based on physical measurements, which might be returning echoes in an ultrasound system, x-ray

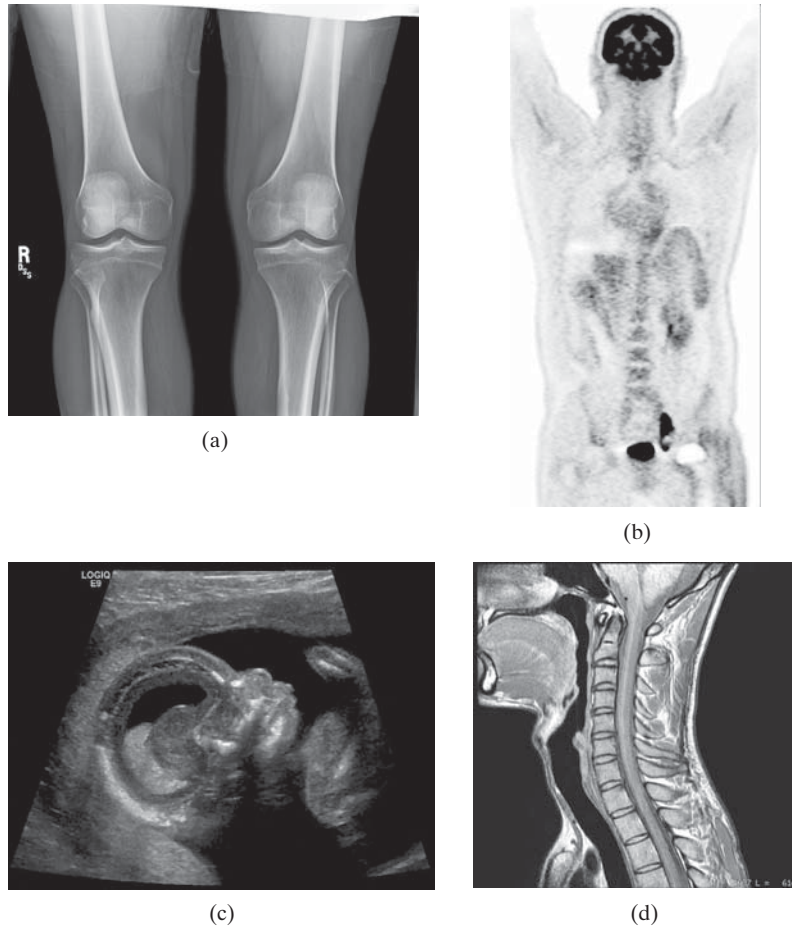


Figure I.1

The four main medical imaging signals discussed in this book: (a) x-ray transmission through the body, (b) gamma ray emission from within the body, (c) ultrasound echoes, and (d) nuclear magnetic resonance induction. The corresponding medical imaging modalities are projection radiography, planar scintigraphy, ultrasound imaging, and magnetic resonance imaging. All images courtesy of GE Healthcare.

intensities in a CT system, or radio frequency waves in an MRI system. The final output in this system is created through *image reconstruction*, the process of creating an image from measurements of signals. The overall quality of a medical image is determined by how well the image portrays the true spatial distribution of the physical parameter(s) of interest within the body. Resolution, noise, contrast, geometric distortion, and artifacts are important considerations in our study of image quality. Ultimately, the clinical utility of a medical image involves both the image's quality and the medical information contained in the parameters themselves.

Figure I.1 shows the four main medical imaging signals discussed in this book: (1) x-ray transmission through the body, (2) gamma ray emission from within the body, (3) ultrasound echoes, and (4) nuclear magnetic resonance induction. Part II covers modalities that use x-ray transmission signals, Part III covers modalities that use gamma ray emission, Part IV covers modalities that use ultrasound signals, and Part V covers magnetic resonance imaging, which uses signals that arise from nuclear magnetic resonance. The specific medical imaging modalities depicted in Figure I.1 are (1) projection radiography, (2) positron emission tomography, (3) ultrasound imaging, and (4) magnetic resonance imaging.

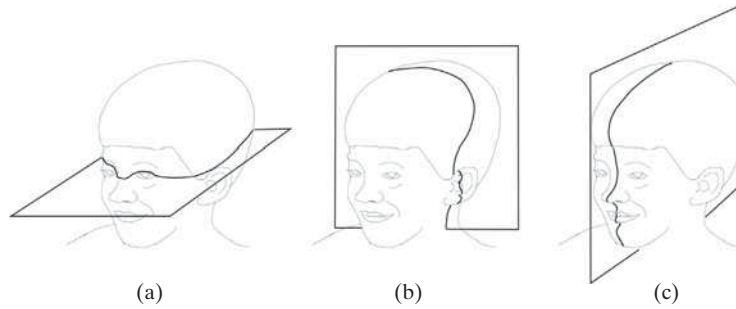
In Figure I.1, parts (a) and (b) represent two-dimensional *projection* images of the three-dimensional human body. A projection is created as a two-dimensional “shadow” of the body, a process that is illustrated in Figure I.2. Figures I.1(c) and (d) are slices within the body. Figure I.3 depicts the three



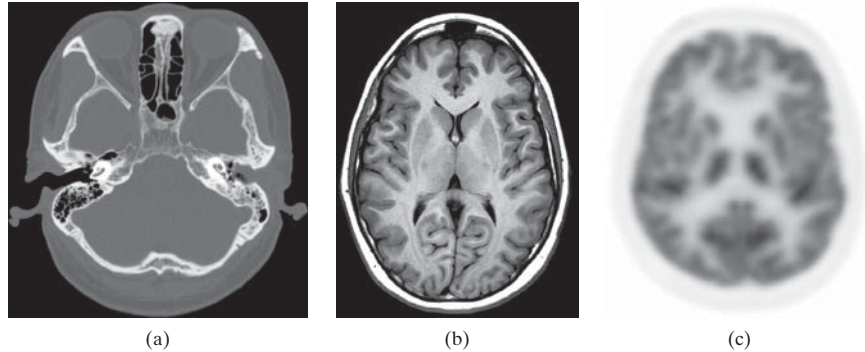
Figure I.2
The creation of a two-dimensional projection through the body. In this case, x-rays are transmitted through a patient creating a radiograph.

Figure I.3

The three standard orthogonal tomographic or slice or section views: (a) axial or transaxial or transverse, (b) coronal or frontal, and (c) sagittal.

**Figure I.4**

Representative transverse slice through the brain from three different imaging modalities: (a) computed tomography, (b) magnetic resonance imaging, and (c) positron emission tomography.



standard orientations of slice (or *tomographic*) images, *axial*, *coronal*, and *sagittal*. Figure I.1(d) is a sagittal slice, while Figure I.1(c) is an *oblique* slice, that is, an orientation not corresponding to one of the standard slice orientations.

Figure I.4 also shows slice images. In this case, each image is a transverse slice, oriented perpendicular to the head and body axis through the brain. Each image is obtained from a different imaging modality: (a) computed tomography, (b) magnetic resonance imaging, and (c) positron emission tomography. Even though each image depicts (a slice through) the brain, the images are strikingly different, because the signals giving rise to each image are themselves strikingly different. In this part of the book, we study the common signal processing concepts that relate to all imaging modalities, setting the groundwork for adding the physical differences that account for the different appearances of the imaging modalities, and hence their different uses in medicine.

Introduction

C H A P T E R

1

In this book, we take a signals and systems approach to the characterization of medical imaging. As discussed in the Overview, there are a variety of signals in which we are interested; ultimately, this interest stems from the biological and medical significance of these signals in patients with various diseases. In practice, these signals are transformed into images via medical imaging modalities. In this chapter, we begin to consider these modalities and their characteristics.

1.1 History of Medical Imaging

The first published medical image was a radiograph of the hand of Wilhelm Conrad Roentgen's wife in December 1895. Roentgen had been experimenting with a Crooke's tube (the forerunner of today's x-ray tube) and noticed that "a new kind of rays" (hence, *x-rays*) were emitted that could expose a photographic plate even when optically shielded. It was immediately obvious to Roentgen that his discovery could have a profound impact in medicine. Indeed, the first clinical use of x-rays occurred only two months later, in February 1896. The use of x-rays became widespread, and both static and dynamic (*fluoroscopic*) techniques were developed. Here, a *static* technique refers to an image taken at a single point in time, whereas a *dynamic* technique refers to a series of images acquired over time.

For many decades, these *planar* (i.e., two-dimensional projection) radiographs were the only medical images being produced. Ultimately, radiography was extended into transmission computed tomography, or *cross-sectional* imaging. Godfrey Hounsfield produced the first true computed tomography (CT) scanner in 1972 at EMI in England. He used mathematical methods for image reconstruction developed a decade earlier by Allan Cormack of the United States. Hounsfield and Cormack shared the Nobel Prize in Medicine in 1979. Many radiologists consider CT scanning to be the most important development in medical imaging since Roentgen's original discovery.

As radiography arose from the discovery of x-rays, nuclear medicine arose from the discovery of radioactivity by Antoine Henri Becquerel in 1896. Initially, radionuclides were used in cancer therapy rather than in medical

imaging. The concept of using radioactive *tracers* to study physiology was introduced by George de Hevesy in 1923; de Hevesy is considered the father of nuclear medicine. A radiotracer is a radioactively labeled drug that mimics a biological compound of interest; the distribution of the radioactivity implies the distribution of the drug. Early studies with radiotracers used conventional nonimaging radiation detectors to roughly determine amounts of radioactivity in various body regions. In 1949, Benedict Cassen at UCLA started the development of the first imaging system in nuclear medicine, the *rectilinear scanner*. The modern *Anger scintillation camera* was developed by Hal Anger at UC Berkeley in 1952. The element of the most commonly used radionuclide in nuclear medicine, technetium-99m, was discovered in 1937 by Carlo Perrier and Emilio Segre; its first use in medicine was in 1961.

The interaction of acoustic waves with media was first described by Lord John Rayleigh over one hundred years ago in the context of the propagation of sound in air. Modern ultrasound imaging had its roots in World War II Navy sonar technology, and initial medical applications focused on the brain. Ultrasound technology progressed through the 1960s from A-mode, B-mode, and M-mode scans to today's two-dimensional (2-D) Doppler, three-dimensional (3-D), and nonlinear imaging systems.

The phenomenon of *nuclear magnetic resonance*, from which magnetic resonance imaging (MRI) arises, was first described by Felix Bloch and Edward Purcell; they shared the 1952 Nobel Prize in Physics. This work was extended by Richard Ernst, who received the Nobel Prize in Chemistry in 1991. In 1971, Raymond Damadian published a paper suggesting the use of magnetic resonance (MR) in medical imaging; in 1973, a paper by Paul Lauterbur followed. Lauterbur received the Nobel Prize in Medicine in 2003, along with Peter Mansfield, who developed key methods in MRI.

1.2 Physical Signals

In this book, we consider the detection of different physical signals arising from the patient and their transformation into medical images. In practice, these signals arise from four processes:

- Transmission of x-rays through the body (in projection radiography and CT)
- Emission of gamma rays from radiotracers in the body (in nuclear medicine)
- Reflection of ultrasonic waves within the body (in ultrasound imaging)
- Precession of spin systems in a large magnetic field (in MRI)

Radiography, CT scanning, and nuclear medicine all make use of electromagnetic energy. Electromagnetic energy or waves consist of electric and magnetic waves traveling together at right angles. Wavelength and frequency are inversely related; frequency and energy are directly related. The electromagnetic spectrum spans the frequency range from zero to that of cosmic rays; only a relatively small portion of this spectrum is useful in medical imaging. At long wavelengths—for example, longer than 1 angstrom—most electromagnetic energy is highly attenuated by the body, prohibiting its exit and external detection. At wavelengths shorter than about 10^{-2} angstroms, the corresponding energy is too high to be readily detected.

In this book, we express energy in units of *electron volts* (eV), where 1 eV is the amount of energy an electron gains when accelerated across 1 volt potential. We will concentrate on electromagnetic radiation whose wavelengths correspond to energies of roughly 25–500 keV.

Ultrasound imaging utilizes sound waves, and considerations of attenuation and detection are similar to those above. Image resolution is not adequate when wavelengths longer than a couple of millimeters are used, and attenuation is too high for very short wavelengths. An ideal frequency range for ultrasound in medical imaging is 1–20 MHz, where 1 Hz = 1 cycle/second.

The signal in MRI arises from the precession (like the motion of a child's top or dreidel) of nuclei of the hydrogen atom—that is, protons. When placed in a large magnetic field, collections of protons, termed *spin systems*, can be set into motion by applying radio frequency (RF) currents through wire coils surrounding the patient. Although these spin systems precess at RF frequencies (64 MHz is typical), the primary signal source is not from radio waves, but from the Faraday induction of currents in the same or different wire coils.

1.3 Imaging Modalities

The medical imaging areas we consider in detail in this book are projection radiography, CT, nuclear medicine, ultrasound imaging, and MRI. An *imaging modality* is a particular imaging technique or system within one of these areas. In this section, we give a brief overview of these most common imaging modalities.

Projection radiography, CT, and nuclear medicine all use ionizing radiation. The first two transmit x-rays through the body, then use the fact that the body's tissues selectively *attenuate* (reduce) the x-ray intensities to form an image. These are termed *transmission* imaging modalities because they transmit energy through the body. In nuclear medicine, radioactive compounds are injected into the body. These compounds or *tracers* move selectively to different regions or organs within the body, emitting gamma rays with intensity proportional to the compound's local concentration. Nuclear medicine methods are *emission* imaging modalities because the radioactive sources emit radiation from within the body.

Ultrasound imaging transmits high-frequency sound into the body and receives the echoes returning from structures within the body. This method is often called *reflection* imaging because it relies on acoustic reflections to create images. Finally, MRI requires a combination of a high-strength magnetic field and radio frequency Faraday induction to image properties of the proton nucleus of the hydrogen atom. This technique is called *magnetic resonance imaging* since it exploits the property of nuclear magnetic resonance.

1.4 Projection Radiography

Projection radiography includes the following modalities:

- *Routine diagnostic radiography*, including chest x-rays, fluoroscopy, mammography, and motion tomography (a form of tomography that is not *computed* tomography)

- *Digital radiography*, which includes all the scans in routine radiography, but with images that are recorded digitally instead of on film
- *Angiography*, including universal angiography and angiocardiology, in which the systems are specialized for imaging the body's blood arteries and vessels
- *Neuroradiology*, which includes specialized x-ray systems for precision studies of the skull and cervical spine
- *Mobile x-ray systems*, which are small x-ray units designed for operating rooms or emergency vehicles
- *Mammography*, which includes film-based or digital-based systems optimized for breast imaging

All of these modalities are called “projection” radiography because they all represent the projection of a 3-D object or signal onto a 2-D image.

The common element in all of these systems is the *x-ray tube*. As we will see in Chapter 5, the x-ray tube generates an x-ray pulse in an approximately uniform “cone beam” (shaped like a cone) geometry. This pulse passes through the body and is attenuated by the intervening tissues. The x-ray intensity profile across the beam exiting from the body is no longer uniform—shadows have been created by dense objects (such as bone) in the body. This intensity distribution is revealed using a scintillator, which converts the x-rays to visible light. Finally, the light image on the scintillator is captured either on a large sheet of photographic film, a camera, or solid-state detectors.

The most common modality in projection radiography is the chest x-ray; a typical unit is shown in Figure 1.1(a). Here, the x-ray tube is located on the column projecting down from the ceiling. The scintillator and detector can be located either in the pedestal unit on the right or in the table itself. The radiologic technologist stands at a console not shown, protected by lead, but able to see through a window. A typical chest x-ray is shown in Figure 1.1(b). This image shows the spine, ribs, heart, lungs, and many other features radiologists are trained to identify and interpret. A key feature of this image is that structures located at different depths in the body are overlaid (or superimposed) on the 2-D image. For example, we can see both front and back ribs in the chest x-ray in Figure 1.1(b). This is a property of projection imaging, and it is common to

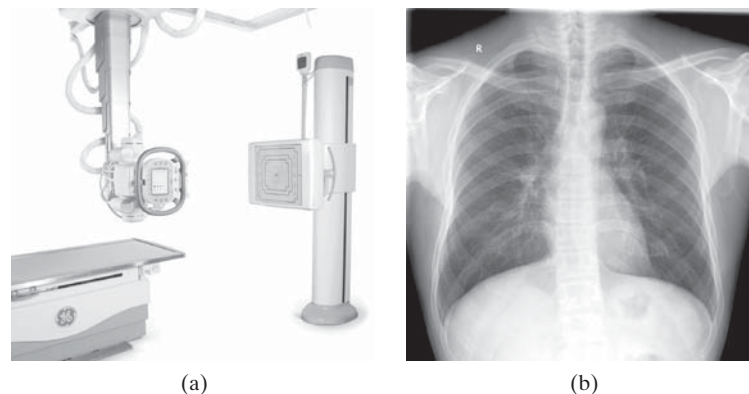


Figure 1.1
 (a) A chest x-ray unit and
 (b) a chest x-ray image.
Source: Courtesy of GE
 Healthcare.

all projection radiographic methods. True *tomography*, the imaging of a 2-D slice of the 3-D body, cannot be directly accomplished using any modality in projection radiography. More details about projection radiography are given in Chapter 5.

1.5 Computed Tomography

As in projection radiography, CT uses x-rays. Unlike projection radiography, however, CT collects multiple projections of the same tissues from different orientations by moving the x-ray source around the body. CT systems have rows of digital detectors whose signals are input directly to a computer, and these signals are used to reconstruct one or more cross sections (slices) of the human body. In this way, although CT systems acquire projections that represent a “shadow” of the body, they generate truly tomographic images after reconstruction.

The important historical phases in CT development are *single-slice CT*, *helical CT*, and *multiple-row detector CT* (MDCT). Single-slice CT systems acquire data within a single plane and reconstruct only one plane per rotation. In helical CT systems, the x-ray tube and detectors continuously rotate around in a large circle, while the patient is moved in a continuous motion through the circle’s center. From the patient’s perspective, the x-ray tube carves out a helix; hence, the name helical CT. The importance of this technique is in its ability to rapidly acquire 3-D data, such as a whole body scan, in less than a minute. In MDCT systems, there are many rows of detectors used to rapidly gather a *cone* of x-ray data, comprising a 2-D projection of the 3-D patient. When the x-ray source and detectors revolve rapidly around the patient (one to two revolutions per second), very quick (near real-time) 3-D imaging is possible using these CT scanners.

A typical CT scanner is shown in Figure 1.2(a). In the center of the picture, we can see the cylindrical opening in which the patient lies; a patient table is also visible. Around the cylindrical opening is a housing containing both the x-ray tube and the detector array. The gantry holding these components is capable of spinning rapidly around the patient. The computer displays and keyboard in the foreground are used for entering patient data and viewing images. Although CT images can be printed on paper or film, the images are completely digital in nature since they are computed from the measured projections. The CT image

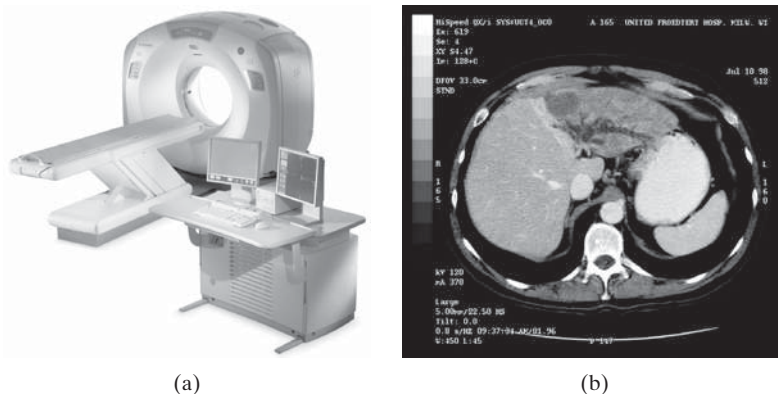


Figure 1.2
 (a) A CT scanner and
 (b) a CT image of a slice
 through the liver.
Source: Courtesy of GE
 Healthcare.